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# DEVELOPMENT OF AN EFFICIENT COMPUTER CODE TO SOLVE THE TIME-DEPENDENT NAVIER-STOKES EQUATIONS

FINAL REPORT

REPORT NO. SR-26

DECEMBER 1975

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FINAL REPORT

REPORT NO. SR-26
DECEMBER 1975

by

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### SUMMARY

A research effort was conducted with the goal of reducing computer time of a Navier Stokes Computer Code for prediction of viscous flow fields about lifting bodies. A two-dimensional, time-dependent, laminar, transonic computer code (STOKES) was modified to incorporate a non-uniform timestep procedure. The non-uniform timestep requires updating of a zone only as often as required by its own stability criteria or that of its immediate neighbors. In the uniform timestep scheme each zone is updated as often as required by the least stable zone of the finite difference mesh. Because of less frequent update of program variables it was expected that the non-uniform timestep would result in a reduction of execution time by a factor of five to ten. Available funding was exhausted prior to successful demonstration of the benefits to be derived from the non-uniform timestep method.

### 2.0 INTRODUCTION

Two elements lie at the core of any satisfactory numerical procedure for computing laminar and/or turbulent transonic airfoil flows, namely, (a) a general method for integrating the equations of continuum mechanics, to which equations governing the evolution of turbulence variables can be added, and (b) a mathematical model that describes the fluctuating component of an arbitrary turbulent field. To the extent possible, both the numerical method and the turbulence model should offer proven reliability; the choices proposed are believed to best meet such a criterion, namely:

- A flow field computer code, which integrates the Navier-Stokes equations in two spatial dimensions, and
- 2. The Saffman Model of turbulent flow.

For each of the many laminar flows (References 1-7) to which it has been applied, the presently operational flow field computer code has been shown to yield solutions accurate enough for any engineering purpose. Furthermore, in the two-dimensional test calculations completed to date, the less proven Saffman turbulence (Ref. 8-9) model, in combination with the flow field computer code, has provided an accurate solution to the turbulent flat plate problem, (Ref. 10) a turbulent boundary layer-shock wave interaction (Ref. 10) and the separation phenomena that occur on a compression corner in supersonic flow. (Ref. 10)

A version of the Afton plane symmetric code (A2P) was developed for the NASA Ames Research Center to solve a laminar transonic airflow problem. The flow field was computed about the lifting NACA 64A410 airfoil at Mach .72, Reynolds number (based on chord length) of 1.75 x 10<sup>6</sup> and at an angle of attack of 4°(ref 11). Starting from the impulsive conditions the calculation was carried out to the time it takes a freestream particle to travel one chord length. The calculation required slightly less than five hours of CDC 7600 computer time. In the course of the calculation the flow separated on the leeward trailing edge, a leeward compression wave formed, and approximately 50% of the measured lift was computed.

However, it was estimated that an additional ten hours on the CDC 7600 computer would be required to complete the problem.

Computing times of the order of fifteen hours on the CDC 7600 to complete one transonic airfoil calculation make transonic flow computations about lifting bodies impractical for design purposes. A speed-up factor of the order of 10 would be necessary for numerical computation of transonic flow to be in the practical range. Coupled with a better estimate of the initial conditions than impulsive inital conditions, and with a speed-up factor of ten, transonic lifting airfoil problems can be solved in less than an hour on the CDC 7600 computer.

The main objective of the work conducted in this program was to develop a computer code wich would be approximately an order of magnitude faster than the present computer program. This was to be accomplished by use of a "Non-Uniform Timestep" in the computation procedure to improve computation efficiency.

# 3.0 SYMBOLS

E	Specific internal energy
j	Index specifying streamline-like direction
k	Index specifying potential-like direction
М	Mass
n	Time index for finite difference equation
p	Pressure
∆t	Timestep increment

# 4.0 NON-UNIFORM TIMESTEP FOR IMPROVMENT IN COMPUTATIONAL EFFICIENCY OF NAVIER STOKES SOLUTIONS

The STOKES computer code was developed for the NASA Ames Research Center from an AFTON plane symmetric code (A2P). It is a two-dimensional time-dependent code used to predict laminar transonic flows about lifting bodies. In common with other AFTON codes, a uniform timestep was incorporated in the original version of the program. The uniform timestep procedure requires that all of the variables of motion in every zone of the mesh be updated or calculated as often as required by stability considerations for the least stable zone of the mesh. The timestep is dependent upon the time required for the speed of sound to cross a zone. It was anticipated that significant computer time savings would be achieved if the non-uniform timestep procedure were incorporated in the code. This allowed the variables of motion to be calculated for a give zone of the finite difference mesh only as often as required by considerations of stability of that zone and its immediate neighbors. It was estimated that a speed-up factor between five and ten would result from the incorporation of non-uniform timestep procedure.

### 4.1 Treatment of Timestep Intermesh Boundaries

One of the most crucial aspects of the non-uniform timestep procedure relates to the way boundaries between adjacent zones having different timesteps are treated. In order to maintain AFTON conservation properties across the interface it had been previously determined by Trulio (Ref. 12) that correct time-centering of the pressures used to update the momenta was essential. As initially conceived, the interface treatment would assume that the adjoining large  $\triangle t$  zone

would be treated in nearly all respects as the small timestep level zone (a micro zone) and updated with a small timestep. In this macro boundary zone the explicitly calculated pressure available from the first microstep update (there would be two such calculations in order to bring the zone correctly forward in time equivalent to a single macrostep calculation) is the correct pressure to use in updating the adjacent momentum zones. This pressure would be used for both microstep momentum updates and the single macrostep momentum update. This procedure would have correctly treated the momentum conservation constraints in the transition from a micro zone to a macro zone.

The method described above does not correctly conserve the total energy in the same transition region. For a macro level zone, j, in the Lagrangian case,

$$M_{i} (E^{n+1}-E^{n-1}) = -p_{i}^{n} \Delta v_{i}^{n}$$
 (1)

must be true toconserve total energy; where  $M_j$  is the zone mass,  $E_j$  the specific internal energy,  $P_j$  the zone pressure and  $\Delta V_j$  the change in volume. Superscripts refer to centering in time; n is a microstep increment. Macrozone energy is updated in time from n-1 to n+1, an interval of 2n or two microsteps. Had we treated this boundary macro zone as a micro zone, as described in Paragraph 2, two such updates would be required.

$$M_{j} (E_{j}^{n} - E_{j}^{n-1}) = p_{j}^{n} \triangle V_{j}^{n}$$
(2)

$$M_{i} (E_{i}^{n+1} - E_{i}^{n} = -P_{i}^{n} \triangle V_{i}^{n})$$
 (3)

The pressure would no longer be correctly centered in relation to the internal energy. The resulting change in internal energy from  $E^{n-1}$  to  $E^{n+1}$  would not be the same as that calculated by Equation (1).

The interface was revised to incorporate a different method which preserves the general conservation properties. Macro zones in the interfaces were to be treated as macro zones in general respects; an intermediate pressure centered at n is calculated in the macro zone and used to update the adjoining momentum zones. This pressure at n is used with Equation (1) to explicitly calculate the internal energy at n + 1 and so preserve total energy conservation. Logic and coding were developed and inserted in the updated program.

### 4.2 Development of Non-Uniform Timestep Logic

The logic for controlling the zone properties updating sequence and the assignment of timestep levels for thermodynamic and momentum zones was included in two new subroutines inserted in the code. These subroutines, ZONEL and TMESTP are shown in the program flow diagram presented in Figure 1. ZONEL is the routine which assigns timestep levels to the thermodynamic and momentum zones. It is called from FLOW at the beginning of a new macrocycle. At that point all zones have been updated to the same time and new levels must be assigned for the new updating sequence.

The TMESTEP subroutive calculates and stores the actual timestep, based upon stability criteria, for each zone. It replaces coding formerly in MVS. This routine is also called from FLOW, but after MVS and after the final macrolevel update. The timesteps are then available for ZONEL to perform its required testing and assignment at the beginning of the next macrocycle. A listing of subroutine ZONEL is included as an Appendix to this report.

The program, as written, is currently restricted to only two timestep levels, although additional ti e reduction should result from multiple time levels. Thus, zones which are at least twice as large as the smallest zone require updating only every other cycle. Zones which are four times larger than the smallest zone would normally require updating only every fourth cycle, etc. A temporary restriction in timestep levels was inserted to simplify checkout and debugging. Coding is in place which will eventually allow up to five timestep levels.

### 4.3 Development of Conservative Logic

In order to maintain the conservative aspects of the AFTON numerical method an approach was taken which utilized momentum and mass accummulators to determine mesh boundary fluxes. This approach, because of its inherent simplicity, offered substantial savings in execution time in addition to the savings which were expected to result from the non-uniform timestep.

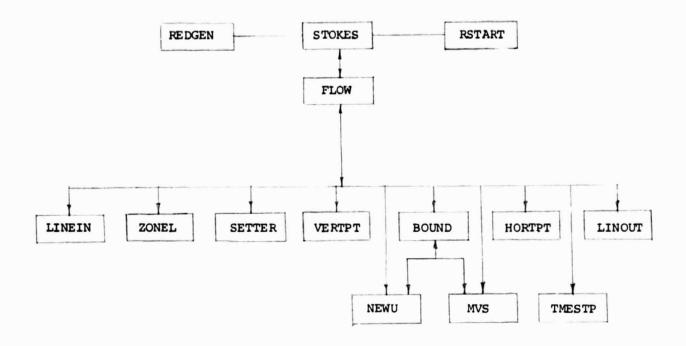


Figure 1: General Flow Diagram for Computer Program With Non-Uniform Timestep Scheme.

Complete conservation also required calculation of the work done on the surfaces of any body placed in the flow field. The AFTON differencing scheme results in a half momentum zone around each of the mesh boundaries and around any body in the mesh. Logic had to be implemented which accounted for the fact that the work calculation for the body surfaces included the momentum transported across these half-zone boundaries.

The various difficulties which were encountered while incorporating the conservation logic eventually led to exhaustion of the available funding for this program. It is estimated that about one-half of the conservation logic had been inserted in the code. Substantial additional programming and debugging effort is required to complete this task and insure that all of the conservation checks of the AFTON method are preserved.

### 4.4 Checkout and Debugging of Non-Uniform Timestep Coding

A test problem was run to check out the code for laminar flow over a right circular cylinder. Three cycles were run with timestep restricted to two timestep levels. The program appeared to execute normally. However, validation of the changes requires completion of the conservation logic and coding.

### 5.0 CONCLUDING REMARKS

An effort was undertaken to incorporate a non-uniform timestep in a two-dimensional, time-dependent, Navier-Stokes solution of the laminar, transonic flow over a lifting body. Available funding was exhausted during the implementation of the conservation logic. Without the conservation properties the accuracy of the numerical calculation is uncertain. Successful demonstration of the non-uniform timestep as a method for improving the efficiency of Navier-Stokes solutions requires additional programming and debugging effort.

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#### APPENDIX

#### Subroutine ZONEL

```
ZONEL. 2
          SUBRUUTINE ZONEL
                                                                                    ZOVEL. 3
  COM* FCOPY
                                                                                    5.405
          PARAMETER MJ=68, MQ=83+295+MJ, IQ=28+MJ
                                                                                    CO4.3
          COMMON SAV(6).TIME, SMOMXI, SMXTPT, SMOMX, SMOMYI, SMYTPT, SMOMY, SEVERI, COM. 4
         1 SIETPT, SKETPT, WURK, SUMIE, SUMKE, SUMTE, FIMPX, FIMPY, SMASSI, SMSTPT,
                                                                                    204.5
                                                                                    CO4.7
         2 SMASS, PROBNU, VZ, GAMMA, EMU, RHOIN, UXIN, UYIN, EIN, OTMM, CUTOFF, NJPA,
         3 NEDIT, N, JMIN, JMAX, KMIN, KMAX, KBOT, KTOP, MAXN, JR, KT, TMAX, JB, J34,
         4 JEM2, KSV(12), NSIG, DTNMN, KMT
                                                                                    C04.8
          CUMMUN A(68),
                            8(65,4),
                                           RX(68,5),
                                                         RY (68.5),
                                                                       UNMX (58,5), CD4,9
                           UNPX(68.5), UNPY(68.5), FMASNM(68.5), FMASN(88.5), CDM, 10
           UNMY (68,5),
         2 ENM(68,5), EN(68,5), PNM(68,5), PN(68,5), PSNMXX(68,5),CDM,11
3PSNMXY(68,5),PSNMYY(68,5), PSNXX(68,5), PSNXX(68,5), PSNYY(68,5),CDM,12
         4 RAASZ(68,5), RHA1Z(68,5), RHAE3Z(68,5), RAAE1Z(68,5),
                                                                       RH3Z(58,5),CO4,13
                                          E12(68,5), RHJ(69,5),
                                                                        VOL(58,5).CO4.14
                           E32(68.5).
         5 FH12(68.5),
                                                         1(6,80)×SA
                                                                         A3x(68,5),C34,15
              £14(68,5),
                            AZX(68,5),
                                          A1X(60,5),
                            A1 Y (68,5),
                                          . (C. 86) YSA
                                                        43Y(68,5),
                                                                         ARX (68,5), CO4.16
              AZY (68,5),
                                          ALY(68,5), DJDX(68 ),
                            ALX (68,5).
                                                                        DJDY(58 ),CO4.17
              ARY (68.5),
            DVDX(68 ), DVDY(68 ), SIGX(68,5), SIGY(68,5), TAUXY(58,5) COM,18
                                                                                    C04,19
          COMMUN
         1 FRNMX (68.5), FRNMY (68.5), FLNMX (68.5), FLNMY (68.5),
                                                                      FMSN2(58,5),CD4.20
         2 FMNMX(68,5), FMNMY(68,5), NTPT(68,5), FMNX(68,5),
                                                                        F4NY(68,5) CD4.21
                                                              LX4,
                                                                                    55,100
                                   LAZ,
          COMMUN
                      L×1.
                                                 LX3.
                                    LINCT.
                                                               ICUN,
                                                                                    C04.23
                                                 NMASS,
                       LX5,
                                    GAMFAC.
                                                 EMUZ.
                                                               DINMPS,
                                                                                    204.24
                       KC.
                                                               CUT,
                       SHATO
                                    CUT1.
                                                 CUT2.
                                                                                    65,403
                       NOMP
                                                                                    15.400
          CUMMON
                                                      LV4.
                                                                LV5.
                                                                          MAXLEV.
                                                                                    85.703
              LEVMX,
                                  LAS.
                                            LV3.
                                                                                    95.400
              MICHO,
                                                                                    C04.30
                                         ACXM(66,5), ACYM(69,5), DTLEV(10 ),
                                                                                    CD4.31
              ACE (68.5).
                            ACM(68,5).
                                                         ZDT (64.5)
                                                                                    CU4.32
              JIF (68.5).
                            JML (65,5),
                                           JZL(65,5),
                                                                                    : 24.55
                                                                                    C04.34
           COMMON NUMBO
                                                                                    CD4.35
           CUMMUN /58LK/ $(36,68),5$(36,68),
                                                                                    CO4.36
          1 NIS.NISS.MINS.NUCH.TM., MI. OM. LM., TM., ETUCM, ENIM. ESTN. STN.
                                                                                    CO4.37
          LAHGE ~ (20000) . MN (20000)
                                                                                    CO4.38
          L = LX3
                                                                                    SUVEL.5
                                                                                    ZOVEL . 6
5
           15 = Lx2
                                                                                    ZONEL. 1
           05 CT UD (1.TD. 3X) 41
L + AIML = 4ML
                                                                                    LIVEL . B
10
           MAXLEV = 2
00 5 M=1,10
                                                                                    ZONEL . 9
11
                                                                                    ZONEL.10
13
           IF (M.GT.MAXLEV) GO TO 4
                                                                                    ZONEL.11
14
           DTLEV(M) = DTNM+(2.4+(M-1))
                                                                                    ZOVEL.12
                                                                                    ZOVEL.13
25
           GU 10 5
                                                                                    LUVEL.14
           DTIEVEM) . 1.
25
                                                                                    LONEL.15
27
     5
           CONTINUE
                                                                                    ZOVEL. 15
           LCT = 0
31
                                                                                    ZUNEL.17
           L = LX1
32
                                                                                    ZOVEL.18
35
           TS= LX>
                                                                                     LOVEL . 19
           60 TU 20
35
                                                                                    STYEL . 20
36
     10
           CUNTINUE
                                                                                    LOVEL . 21
           F = FXS
```

ZONEL

```
ZUNEL 37
                                                           L5 = LX1
GU TU 20
CONTINUE
                                                                                                                                                                                                                                                                                                                           SOVET'SS
                                                                                                                                                                                                                                                                                                                           ZUVEL. 23
                                                                                                                                                                                                                                                                                                                           ZOVEL.24
                                                            L = Lx3
                                                                                                                                                                                                                                                                                                                           ZOVEL.25
                                                                                                                                                                                                                                                                                                                           ZONEL.26
                                                            CONTINUE
                                                                                                                                                                                                                                                                                                                           LUNEL.27
                                                            LCT = LC1 + 1
DO 50 J = JMIN, JR
                                                                                                                                                                                                                                                                                                                            LOVEL. 28
                     47
                                                            IF(J.E3.JBM) GO TO 50
IF(ZDT(J,L) .GT. DTLEV(2)) GO TO 25
                     52
                                                            JZL(J,L) = 1
GO TO 50
                     60
                     61
                                                            TEMPORY COMMENT OUT OF TRANSFER TO LIMIT TO TWO LEVELS

IF(ZDT(J,L),GT,DTLEV(3)) GO TO 30
                                     C25
                                                    20NEL.35
20NEL.37
20NEL.39
20NEL.39
20NEL.39
20NEL.40
20NEL.41
20NEL.42
20NEL.42
20NEL.43
20NEL.44
20NEL.45
20NEL.44
20NEL.45
20NEL.46
20NEL.46
20NEL.46
20NEL.46
20NEL.47
20NEL.46
20NEL.47
20NEL.48
20NEL.49
20NEL.49
20NEL.49
20NEL.49
20NEL.50
20NEL.50
20NEL.50
20NEL.50
20NEL.50
20NEL.50
20NEL.51
20NEL.52
20NEL.53
20NEL.54
20NEL.54
20NEL.55
20NEL.55
20NEL.55
20NEL.56
20NEL.56
20NEL.56
20NEL.65
20N
                     62
                                        25
                                                            CONTINUE
                     62
                     66
                     70
                     77
                 105
                  100
                  107
                                     40
                  107
                                     50
                 113
                 116
                 120
                 132
                 133
                 155
                 150
                 172
                 204
                 207
                 211
                                     61
                                    C
                                    C
                                    C
                214
                                        62
                                                           CONTINUE
                214
                                                           J1= J9 - 2
                 215
                 217
                                                            J3 = J8
                 550
                                     621 CONTINUE
                                                           JML(J1.L) = MINO(JZL(J3,L),JZL(J2,L5),JZL(J3,L5))
                 240
                                                           IF (JI. NE. Je) GO TO 60
                                                                                                                                                                                                                                                                                                                           CO.JBVCS
                242
                 243
                                                           J2 = J8M + 1
                                                                                                                                                                                                                                                                                                                            ZOVEL.70
                 244
                                                           J3 = J9M - 1
                 245
                                                           60 IN 951
                                                                                                                                                                                                                                                                                                                           ST.Jarch
                                    C
                                                           SPECIAL TESTING FOR KLINES AHOUND THE BUDY
                                    C
                                                                                                                                                                                                                                                                                                                           ZONEL . 74
                                    C
                                                                                                                                                                                                                                                                                                                          ZOVEL.75
                245
                                                           CONTINUE
                                       63
                                                                                                                                                                                                                                                                                                                           ZJ VEL. 76
                 245
                                                           J1= J8
```

# ORIGINAL PAGE IS OF POOR QUALITY

```
ZONEL
    240
                                                                                                ZUNEL.75
    250
            631 CONTINUE
                                                                                                ZUNEL.79
                  JML(J1.L) = MINO(J2L(J2.L),J2L(J2.L5))
     250
                                                                                                ZUNEL. BO
                 1F(J1.NE.JB) GO TO 65
     503
                                                                                                18. Jakes
    265
                 J1= J84
                                                                                                SA'TBAO?
                 J2 = JBM - 1
                                                                                                ZONEL. 83
    200
                 GO TU 631
    207
                                                                                                ZONEL. 84
                                                                                                ZOVEL. 85
                 SPECIAL TESTING FOR KTOP
                                                                                                LONEL, 85
                                                                                                ZONEL.87
    270
           64
                 CONTINUE
                                                                                                ZUNEL. 88
                 J1 = J8 - 2
    270
                                                                                                LOVEL.89
     271
                                                                                                LIVEL. 70
     275
                  J3 = J8
                                                                                                ZONEL. 91
           641 CONTINUE
     274
                                                                                                SONEL.92
                 JML(J1,L) = MINO(J2L(J3,L),JZL(J3,L5),J2L(J2,L))
    274
                                                                                                LOVER 93
                 IF (J1 .NE . JA) GO TO 66
                                                                                                LONEL. 94
     313
                                                                                                ZONEL 95
ZONEL 96
ZONEL 97
ZONEL 98
                 J1= J8M
J2= J8M + 1
J5= J8M - 1
     315
     310
     317
                 GO TU 641
     320
     320
                 CONTINUE
                 J1= J8
J2= J8 - 2
     320
                                                                                                ZONEL.100
     321
                                                                                                ZONEL. 101
     323
                  J3 = J8
                                                                                                ZOVEL.102
           651 CONTINUE
                                                                                                ZOVEL, 103
     324
                 JML(J1,L) = MINO(JZL(J2,L),JZL(J3,L),JZL(J2,L5),JZL(J3,L5))
     324
                                                                                                ZONEL.104
     351
                 IF (J1. NE. JB) GD TO 66
                                                                                                ZOVEL.105
     353
                                                                                                ZONEL.106
                  J1= J84
                 J2 = J8M - 1
J3 = J8M + 1
     354
                                                                                                ZONEL.107
     355
                                                                                                ZONEL. 108
                  GO 10 651
                                                                                                ZOVEL.139
     350
     350
                 CONTINUE
                                                                                                ZUNEL.110
           66
     350
                 IF (LCT.NE.2) GO TO 68
                                                                                                ZUNEL,111
     360
                 L = LXI
                                                                                                ZOVEL.112
                 15 = FX5
    361
                                                                                                ZONEL,113
                 DO 67 J = JMIN, JR
JML(J, L) = JML(J, L2)
     353
                                                                                                ZOVEL.114
     674
           67
                                                                                                ZONEL.115
     176
                 GU TU 69
                                                                                                ZOVEL.116
                 F = Fx5
     577
                                                                                                40 VEL . 117
                                                                                                20 . L. 118
     400
    402
                  CUNTINUE
                                                                                                ZONEL.117
     402
                 DG 70 J = JMIN, JH
                                                                                                ZOVEL.120
    404
                 IF (J.Eq. JBM) Go TO 70
                                                                                                191.19102
                 JP = J + 1
JTMP = MINO(JML(J,L) , JML(J,L2),JML(JP,L),JML(JP,L2))
IF(JTMP,EQ,J/L(J,L)) GO TO 70
    420
                                                                                                101EP 155
                                                                                                SOVEL . 153
    421
                                                                                                ZONEL.124
     430
                 JIF (J, L) = 1
    435
                                                                                                251.13VCL
                  JZL(J.L) = JTMP
                                                                                                ZUNEL.126
     456
                 CONTINUE
                                                                                                20 VEL . 127
     437
     442
                  IF (LCT. EQ. 2) GO TO 15
                                                                                                43 .EL. 128
     444
                  HETURN
                                                                                                LOVEL.129
     444
                 END
                                                                                                LUNEL.130
```

